02417: Time Series Analysis Week 1 - Introduction and overview

Peder Bacher DTU Compute

Based on material previous material from the course

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Material in the course

- The course webpage 02417.compute.dtu.dk
- Learn for messages and projects
- Book
- Slides
- Exercises
- Assignments

What to use Time Series Models for

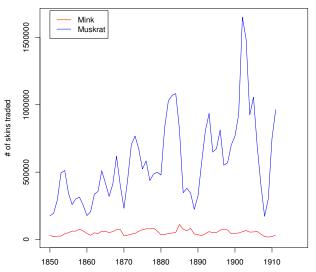
Applications:

- Prediction
- Estimation and hypothesis testing
- Control and decision making

We want a good model!

- Use data to fit a model
- Basically, any modelling technique can be used, there are no rules!
- Pros and cons: robustness, complexity, computation time, man hours to set up, ...
- WE ONLY DO LINEAR MODELS in this course (multiply and add using matrices)! Very fast and reliable, always a good starting points when developing models, can be tweaked later to include non-linear effects...

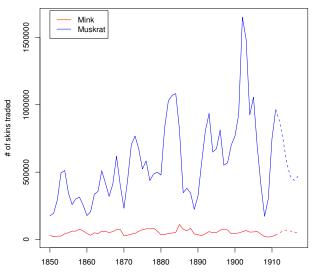
What you should be able to do



Mink and Muskrat skins traded in Canada 1850–1911

Years

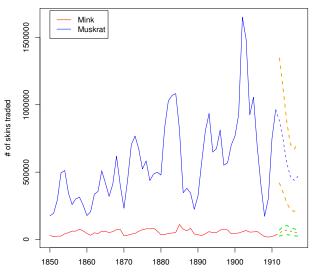
What you should be able to do



Mink and Muskrat skins traded in Canada 1850–1911

Years

What you should be able to do



Mink and Muskrat skins traded in Canada 1850–1911

Years

Introductory example – shares (COLO B 1 month)



What do think about the trend here? what would you buy or sell?

Introductory example – shares (COLO B 1 year)



Would you do the same?

Introductory example – shares (COLO B all)



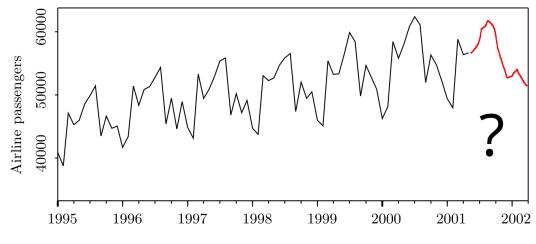
Can we use a linear trend model here?

Introductory example – shares (COLO B log(all))



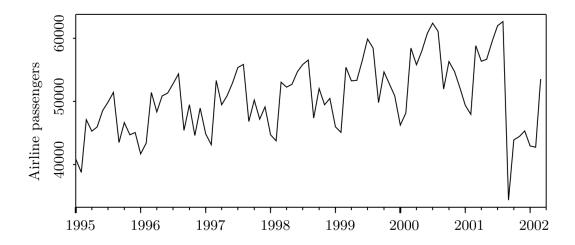
Take log(y): Often we can do non-linear transformations, resolve in cos and sine or splines,...

Number of Monthly Airline Passengers in the US

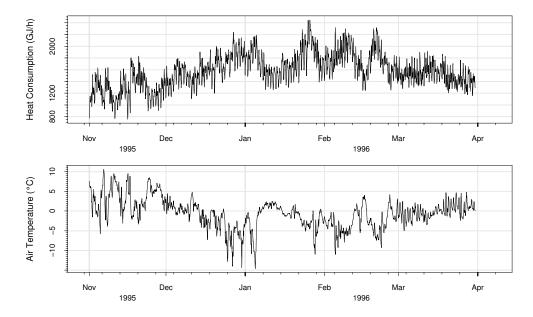


Is this a good prediction?

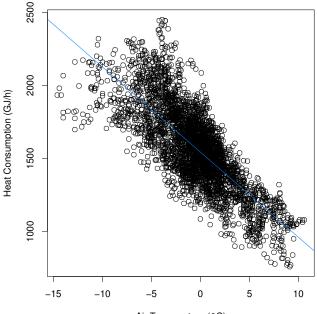
Number of Monthly Airline Passengers in the US



Consumption of District Heating (VEKS) - data



Consumption of DH – simple model



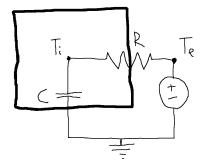
Discussion: What is a dynamical system?

Last year!



Simplest first order RC-system

Single state model of the temperature in a box:





Discretize the ODE

$$\frac{dT_{\rm i}}{dt} = \frac{1}{RC} (T_{\rm e} - T_{\rm i})$$

It has the solution

$$T_{\mathrm{i}}(t + \Delta t) = T_{\mathrm{e}}(t) + e^{-rac{\Delta t}{RC}} \left(T_{\mathrm{i}}(t) - T_{\mathrm{e}}(t)\right)$$

if $\Delta t = 1$ and $T_{\rm e}$ is constant between the sample points then

$$T_{t+1}^{i} = e^{-\frac{1}{RC}} T_{t}^{i} + (1 - e^{-\frac{1}{RC}}) T_{t}^{e}$$

since $e^{-\frac{1}{RC}}$ is between 0 and 1, then write it as

$$T_{t+1}^{\mathbf{i}} = \phi_1 T_t^{\mathbf{i}} + \omega_1 T_t^{\mathbf{e}}$$

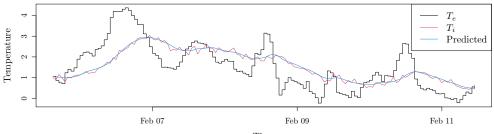
where ϕ_1 and ω_1 are between 0 and 1.

Add a noise term and we have the ARX model

$$T_{t+1}^{i} = \phi_1 T_t^{i} + \omega_1 T_t^{e} + \varepsilon_{t+1} T_t^{i} = \phi_1 T_{t-1}^{i} + \omega_1 T_{t-1}^{e} + \varepsilon_t$$

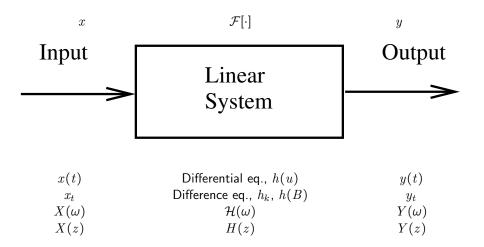
An ARMAX model

$$T_t^{i} = \phi_1 T_{t-1}^{i} + \omega_1 T_t^{e} + \varepsilon_t + \theta_1 \varepsilon_{t-1}$$

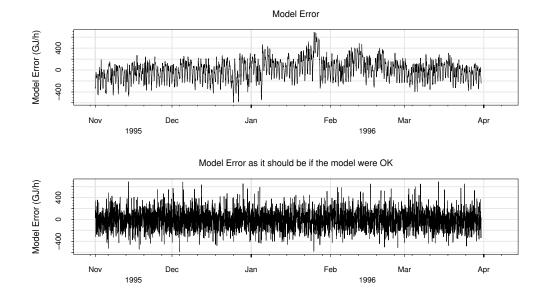




Linear Dynamic Systems – notation



Consumption of DH – We use the model error to validate the model



A brief outline of the course

- General aspects of multivariate random variables
- Prediction using the general linear model
- Time series models
- Some theory on linear systems
- Time series models with external input

Some goals:

- Characterization of time series / signals; correlation functions, covariance functions, stationarity, linearity, ...
- Signal processing; filtering and smoothing
- Modelling; with or without external input
- Prediction with uncertainty