

# Mandatory Exercise: Persistent Data Structures

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**1 Use of persistence** Use **persistent** data structures to describe an efficient and simple solution to each of the following problems.

**1.1** Given a set  $I$  of  $n$  intervals  $\{[x_1, y_1], [x_2, y_2], \dots, [x_n, y_n]\}$  on the real line, build a data structure that efficiently supports the following query:

- *contains*( $p$ ): return all intervals in  $X$  that contain the point  $p$ .

**1.2** Given a set  $L$  of  $n$  line segments in the plane all parallel to the  $x$ -axis, build a data structure that supports the following query:

- *intersect*( $s$ ): Return all segments in  $L$  that intersect  $s$ , where  $s$  is a line segment parallel to the  $y$ -axis.

The segment  $s$  is given on the form  $(x, y_1, y_2)$  and the line segments in  $L$  are given on the form  $(x_1, x_2, y)$ .

Analyze the space, preprocessing time, and query time of your solutions.