

# Exercises — A-not A and same-different tests in `sensR`

Christine Borgen Linander

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## Topics:

Analysis of data from the protocols

- A-not A
- Same-different
- A-not A with sureness

## Exercise 1

You have conducted an A-not A experiment with 100 subjects. The answers are summarized in table 1.

Table 1: A-not A data for exercise 1.

Sample	Response		Total
	“A”	“not A”	
A	57	43	100
Not A	42	58	100

1. Have you shown that the A and not-A products are different?
2. Have you shown that the A and not-A products are similar (using  $d' = 0.75$  as the boundary of similarity) at the 5% level?
3. Have you shown that the A and not-A products are similar at the 1% level (again using  $d' = 0.75$  as the boundary of similarity)?

## Exercise 2

It has come to you knowledge that the technicians undertaking the test formulated the question in the following manner:

“You are now given two samples and you are asked to determine if these samples are the same or not. Answer *A* if you believe the samples are the same and *not A* if you believe they are not the same”

As you may realize, these are the instructions for the same-different test rather than the A-not A test, and we will have to analyze the data assuming the same-different cognitive decision rule rather than that of the A-not A.

1. Estimate  $d'$  assuming the same-different protocol instead of the the A-not A protocol. Does the estimate of  $d'$  change? and if so, is it a large difference or a small unimportant one?
2. What is the  $p$ -value of the test of “no product difference”? Compare this to the  $p$ -value obtained using the A-not A test. Has the  $p$ -value changed? Is it important?
3. Make a similarity analysis similar to the one for the A-not A analysis. Are there any differences?
4. At what boundary-of-similarity ( $d'_0$ ) are you able to declare the products 'similar' at the 5% level?

### Exercise 3

You have conducted a large-scale consumer study using the A-not A with sureness protocol and obtained the data in the following table.

	sureness					
prod	1	2	3	4	5	6
ref	10	40	70	50	20	10
test	20	30	20	30	60	40

To get the data into R you may use the following commands:

```
> wts <- c(10, 40, 70, 50, 20, 10, 20, 30, 20, 30, 60, 40)
> dat <- data.frame(sureness = factor(rep(1:6, 2), ordered=TRUE),
+                   prod = factor(rep(c("ref", "test"), each = 6)),
+                   freq = wts)
> dat
```

	sureness	prod	freq
1	1	ref	10
2	2	ref	40
3	3	ref	70
4	4	ref	50
5	5	ref	20
6	6	ref	10
7	1	test	20
8	2	test	30
9	3	test	20

```
10      4 test  30
11      5 test  60
12      6 test  40
```

```
> ## Tabulate the data:
> xtabs(freq ~ prod + sureness, dat)
```

```
      sureness
prod   1  2  3  4  5  6
ref  10 40 70 50 20 10
test 20 30 20 30 60 40
```

1. First assume that there is no difference in scale: compute  $d'$  using the `c1m` function. Also compute the *sensitivity* and the overlap of the perceptual distributions.
2. Test if the products are different assuming the equal-variances model.
3. Now fit the model that allows for differences in scale/unequal variances for the two products.
4. Test if the variances are different or whether they can be assumed to be equal.
5. Test if products are different in the unequal-variances model and compare results to the question 2.
6. Compute  $d'$ , the scale-ratio (i.e. the standard deviation of the 'test' distribution assuming the standard deviation of the 'reference' distribution is 1), the sensitivity and the overlap of the perceptual distributions.
7. Compare and discuss differences and similarities in  $d'$ , sensitivity and distribution overlap.