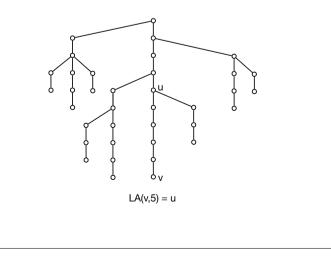
### Level Ancestor

- Level Ancestor Problem
- Trade-offs

Philip Bille

### Level Ancestor

- Level ancestor problem. Preprocess rooted tree T with n nodes to support
  - LA(v,k): return the kth ancestor of node v.



### Level Ancestor

#### • Applications.

- Basic primitive for navigating trees (any hiearchical data).
- Illustration of wealth of techniques for trees.
  - · Path decompositions.
  - Tree decomposition.
  - Tree encoding and tabulation.

# Level Ancestor

- Level Ancestor Problem
- Trade-offs

### Level Ancestor

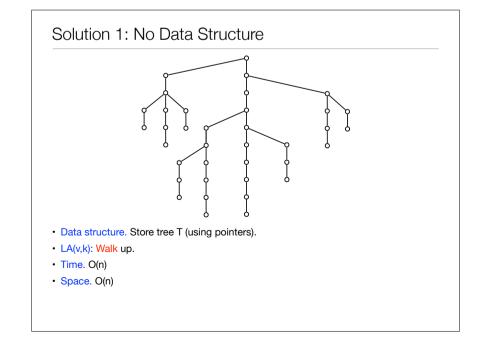
- Level Ancestor Problem
- Trade-offs

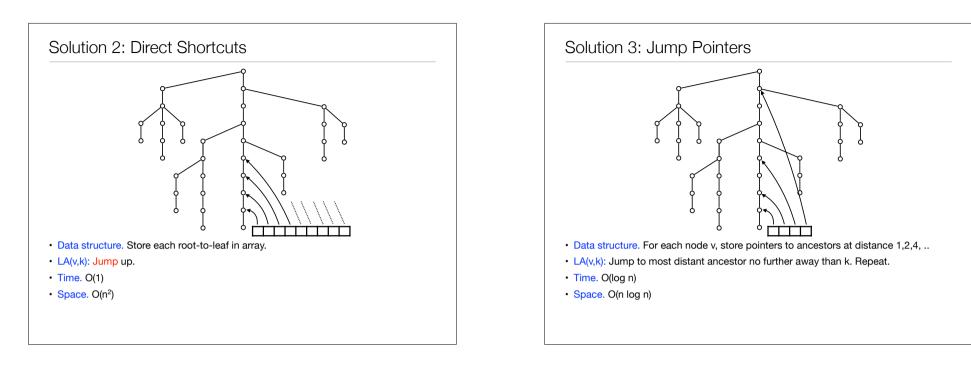
### Level Ancestor

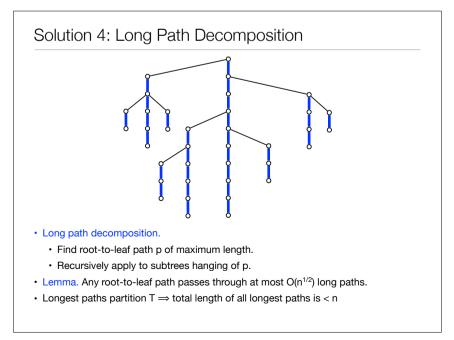
Solutions?

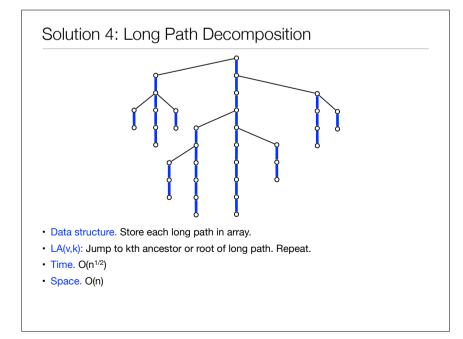
#### Level Ancestor

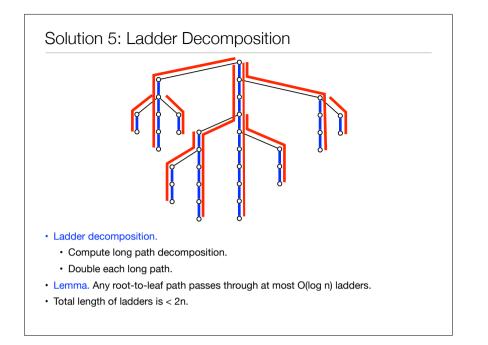
- Goal. Linear space and constant time.
- Solution in 7 steps (!).
  - No data structure. Very slow, litte space
  - Direct shortcuts. Very fast, lot of space.
  - ....
  - Ladder decomposition + jump pointers + top-bottom decomposition. Very fast, little space.

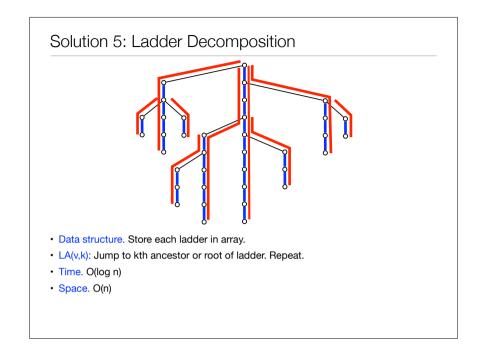


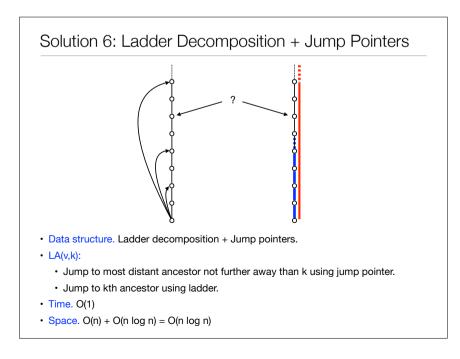


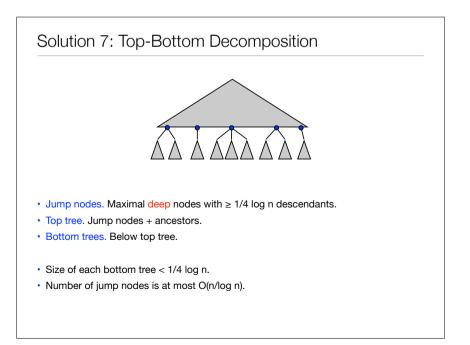


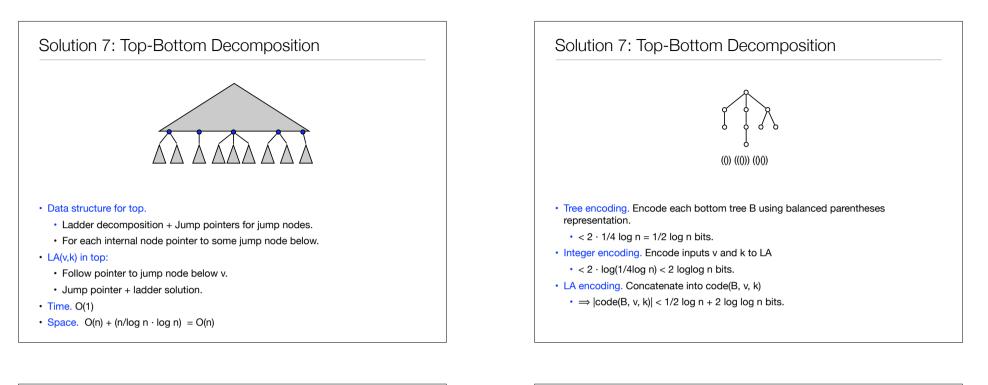


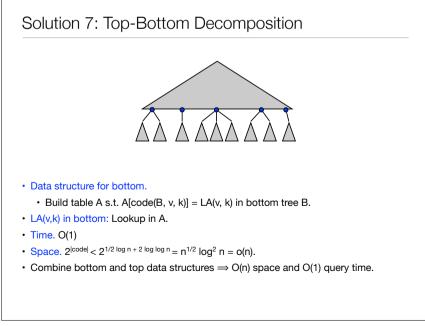












### Solution 7: Top-Bottom Decomposition

• Theorem. We can solve the level ancestor problem in linear space and constant query time.

## Level Ancestor

- Level Ancestor Problem
- Trade-offs